

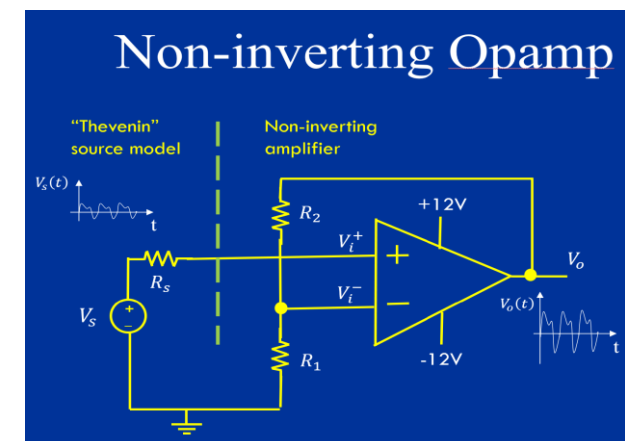
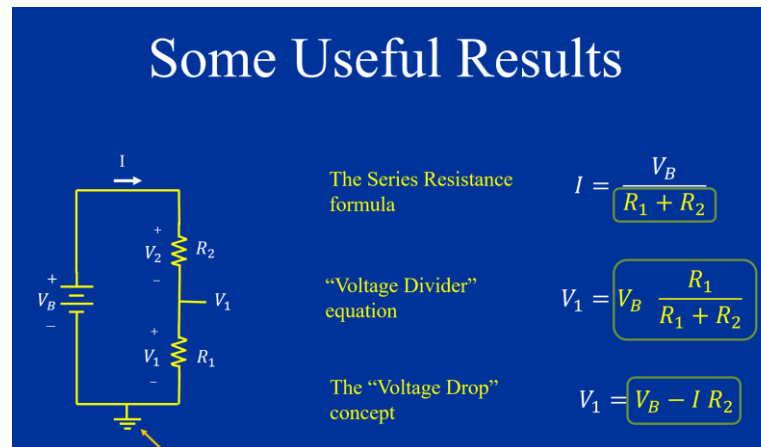
ECE Topics #3 - Circuit Analysis – From Theory to Applications

Slides downloaded from: <https://ecefiles.org/ece-topics/>

Companion video at: <https://www.youtube.com/watch?v=8UBXjlilkeU>

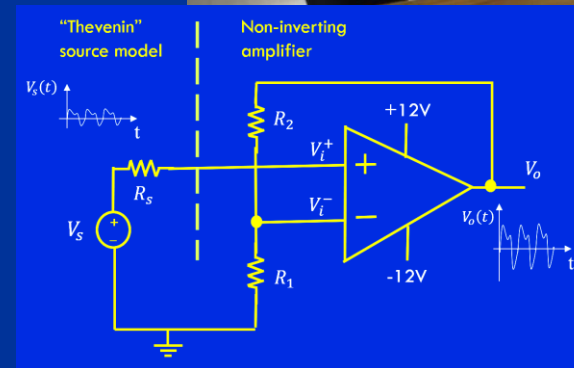
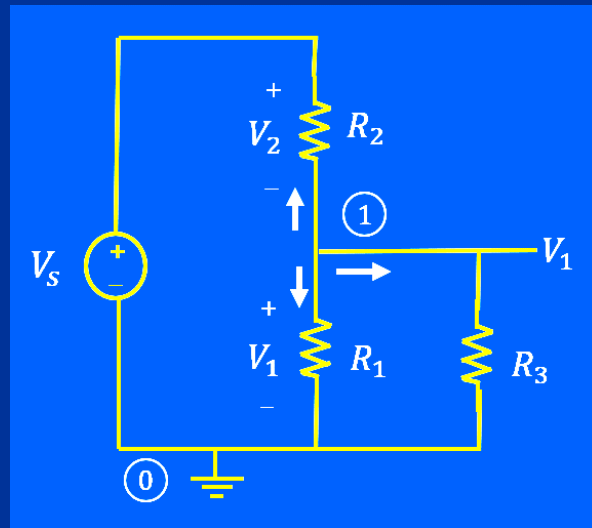
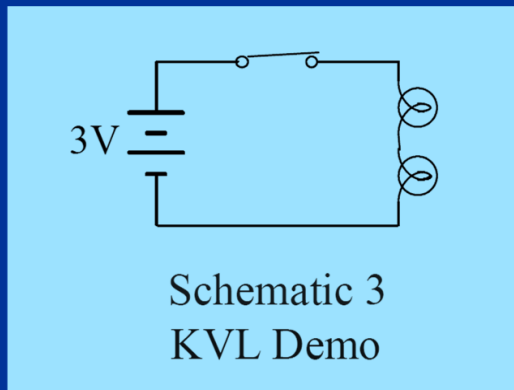
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This video focuses on how fundamental theory like Kirchoff's Laws are used to analyze, understand, and design real-world products. Basic topics include Ohm's Law, KVL, KCL, Nodal Analysis, the ubiquitous voltage divider circuit, and more. But the main theme is how these give way to analysis using common subcircuits, leveraging known results. While a guitar amp and DSP reverb are used in demos, the topics covered are essential to all analog circuit analysis. The design of a voltage amplifier built using an opamp is also discussed.



Topics in ECE #3

Circuit Analysis Theory and Applications



Demo in Lecture Class



CAUTION!
120 VAC



Typical Undergrad EE Curriculum

Freshman year

Fall semester (16 credit hours)

- CHM 210 - Chemistry I **Credits:** (4)
- COMM 105 - Public Speaking IA **Credits:** (2)
- ECE 015 - New Student Assembly **Credits:** (0)
- ECE 210 - Introduction to Electrical Engineering **Credits:** (3)
- ENGL 100 - Expository Writing I **Credits:** (3)
- MATH 220 - Analytic Geometry and Calculus I **Credits:** (4)

Spring semester (17 credit hours)

- BIOL 198 - Principles of Biology **Credits:** (4)
- or
- CHM 230 - Chemistry II **Credits:** (4)
- ECE 115 - New Student Design Project **Credits:** (1)
- ECON 110 - Principles of Macroeconomics **Credits:** (3)
- MATH 221 - Analytic Geometry and Calculus II **Credits:** (4)
- PHYS 213 - Engineering Physics I **Credits:** (5)

Sophomore year

Fall semester (17 credit hours)

- CHE 354 - Basic Concepts in Materials Science and Engineering **Credits:** (1)
- CHE 356 - Fundamentals of Electrical Properties **Credits:** (1)
- ECE 241 - Introduction to Computer Engineering **Credits:** (3)
- ECE 410 - Circuit Theory I **Credits:** (3)
- MATH 240 - Elementary Differential Equations **Credits:** (4)
- PHYS 214 - Engineering Physics II **Credits:** (5)

Spring semester (16 credit hours)

- CIS 209 - C Programming for Engineers **Credits:** (3)
- ECE 511 - Circuit Theory II **Credits:** (3)
- ECE 525 - Electronics I **Credits:** (3)
- MATH 222 - Analytic Geometry and Calculus III **Credits:** (4)
- STAT 510 - Introductory Probability and Statistics I **Credits:** (3)

Junior year

Fall semester (16 credit hours)

- **Humanities/Social Science Elective **Credits:** (3)
- ECE 431 - Microcontrollers **Credits:** (3)
- ECE 526 - Electronics II **Credits:** (3)
- ECE 540 - Applied Scientific Computing for Engineers **Credits:** (3)
- ECE 557 - Electromagnetic Theory I **Credits:** (4)

Spring semester (17 credit hours)

- **Humanities/Social Science Elective **Credits:** (3)
- ECE Technical Electives **Credits:** (3)
- ECE 502 - Electronics Laboratory **Credits:** (2)
- ECE 512 - Linear Systems **Credits:** (3)
- ECE 581 - Energy Conversion I **Credits:** (3)
- ENGL 415 - Written Communication for Engineers **Credits:** (3)

Senior year

Fall semester (15 credit hours)

- ***Technical electives **Credits:** (6)
- CE 530 - Statics and Dynamics **Credits:** (3)
- ECE 530 - Control Systems Design **Credits:** (3)
- ECE 590 - Senior Design Experience **Credits:** (3)

Spring semester (15 credit hours)

- ***Technical electives **Credits:** (9)
- **Humanities/Social Science Elective **Credits:** (3)
- ME 513 - Thermodynamics I **Credits:** (3)

Electrical engineering options

General option

Intro EE and Electronics

Introduction to Electrical Engineering Syllabus

Prerequisites: Good background in algebra. Some calculus and complex number experience is handy, but we'll introduce these as needed.

Course Description:

Classically, ECE students had to wait till the 2nd semester of their Sophomore year to take circuit theory, and till their *Junior year* to get into an EE lab. This course changes all that, giving incoming students a chance to experience electrical engineering in their first year.

It is a moderately rigorous course designed as an introduction to fundamental electrical engineering concepts that you will use for the rest of your life. In it you will learn the basics of EE as well as practical knowledge about the world's electrical infrastructure and modern electronic products.

Course Topics:

- AC and DC voltages, currents, power, and essential circuit theory concepts.
- Oscilloscopes, function generators, and meters.
- Circuit fabrication techniques, including breadboard construction and soldering.
- Opamps, transistors, and integrated circuit fundamentals and applications.
- Lab experiments including covering real-world applications including, batteries, switches, microphones and loudspeakers, motors and generators, amplifiers, etc.

Labs: Labs meet once per week (nominally)

This is an integral part of the course, and accounts for a major part of your grade.

Lab Kit: You will need to purchase a lab kit (approx. \$40) that contains the core components required to complete the projects. **This must be purchased by the second week of the semester.**

Tools: As you begin your Electrical Engineering career, you should begin to collect some basic tools. These include wire cutters, strippers, needle-nose pliers, a soldering iron, etc. Your professor or lab instructor can give you information on where and how to purchase these. (Purchase is somewhat optional, but strongly encouraged).

Electronics II Syllabus

Prerequisites: Electronics I and Circuit Theory II

Required Text: A.S. Sedra & K.C. Smith, **Microelectronic Circuits**, Oxford, 2010.

Resources: **Practical Electronics for Inventors**, Paul Scherz and Simon Monk, Copyright 2016, McGraw Hill. This is an amazing book for the money. It contains a wealth of schematics and reference information that is complementary to the deeper theoretical info in our course text.

Course Description:

This course builds on previous circuits and electronics courses, providing the theory needed to understand and design practical circuits/systems of moderate complexity.

While the textbook concentrates on classic low-level design, we will also cover topics not in that book, including switch-mode power supplies, modern IC components, and interfacing to and from microprocessors with analog-to-digital and digital-to-analog converters.

Part I (The big picture)

- ◆ Review of amplifier models, including gain, R_{in} , R_{out} , loading, and frequency response
- ◆ Frequency domain characterization of real-world signals with examples (Fourier theory)
- ◆ Opamps, including modern single-supply circuits, low-voltage, low-power ICs, and data-sheets
- ◆ Additional analog ICs (comparators, switches, regulators, ADCs/DACs, etc.)
- ◆ Example systems that include amplifiers, ADCs, DACs, and digital signal processing (DSP).
- ◆ Circuit board layout, including power and signal integrity, and EM compatibility issues

Part 2 (Elaboration of discrete devices and common sub-circuits used in designing analog and digital ICs)

- ◆ Diodes, classic power supplies, and modern switching supplies
- ◆ Review of MOSFET structure and operation with switching and amplifier circuit examples
- ◆ Amplifier configurations (e.g. CS, CG, CD, and high-frequency behavior)
- ◆ Multi-transistor amplifiers, Miller's theorem, and cascoding/buffering to improve frequency response.
- ◆ Comparison of MOSFETs and BJTs.
- ◆ Power dissipation and heat-sinking
- ◆ Differential amplifiers, power-amp stages, and basics of op-amp internal designs
- ◆ Feedback, and stability

Additional topics will be interwoven as time permits (e.g. Simulators, filter design, IC design, etc.)

Homework: There will be approximately 8 to 10 homework assignments throughout the semester, most of which will be collected and graded.

Today's Topics

- Quick review from Episode 1
- Using Kirchhoff's Laws
- Analysis using Equivalent Circuits
- Subcircuit recognition and understanding

Ohm's and Kirchhoff's Laws...

Ohm's Law

$$I = \frac{V}{R}$$
$$V = IR$$
$$R = \frac{V}{I}$$

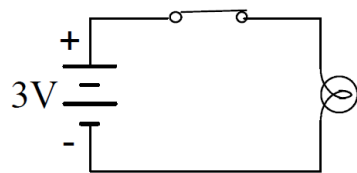
Kirchoff's Current Law
At a "node":

$$\sum I_{entering} = \sum I_{leaving}$$

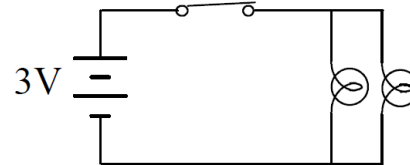
Kirchoff's Voltage Law
Around a loop:

$$\sum V_{rises} = \sum V_{drops}$$

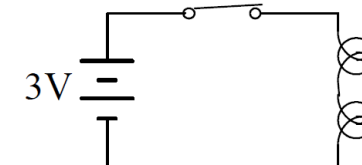
In this lab, we will build 3 simple circuits, shown in the 3 schematics below.



Schematic 1
Ohm's Law Demo

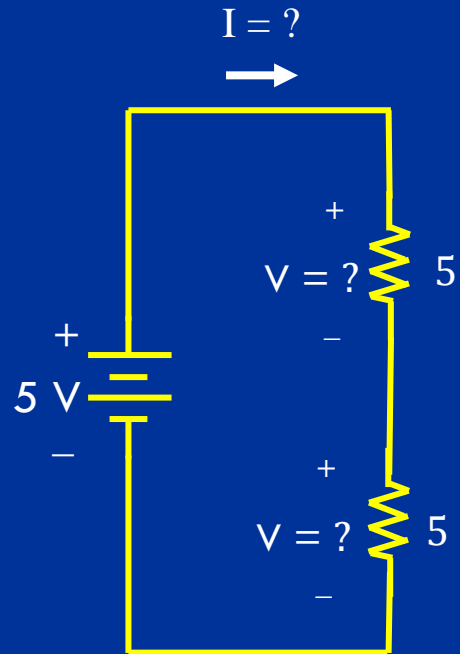


Schematic 2
KCL Demo

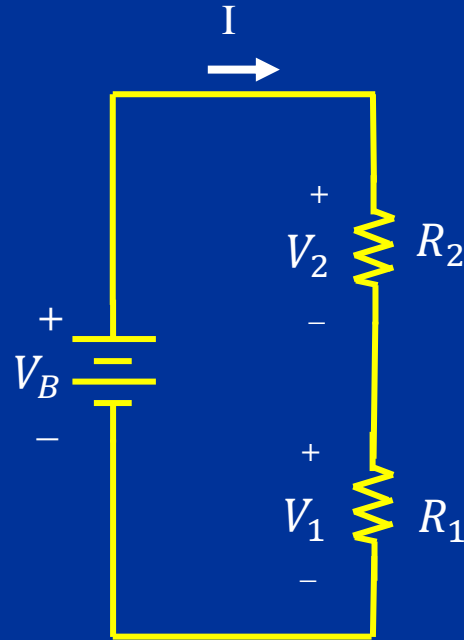
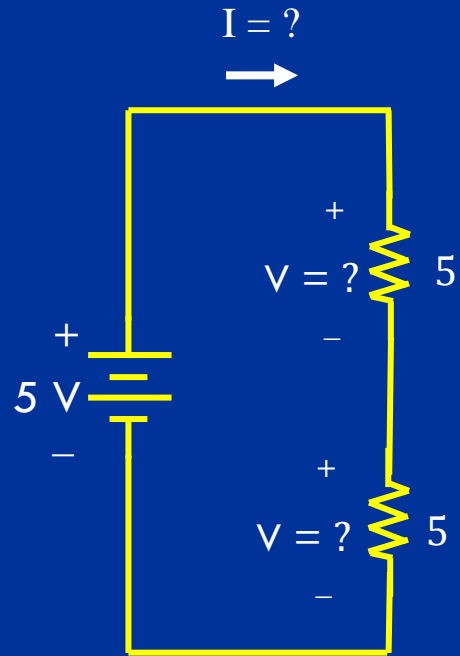


Schematic 3
KVL Demo

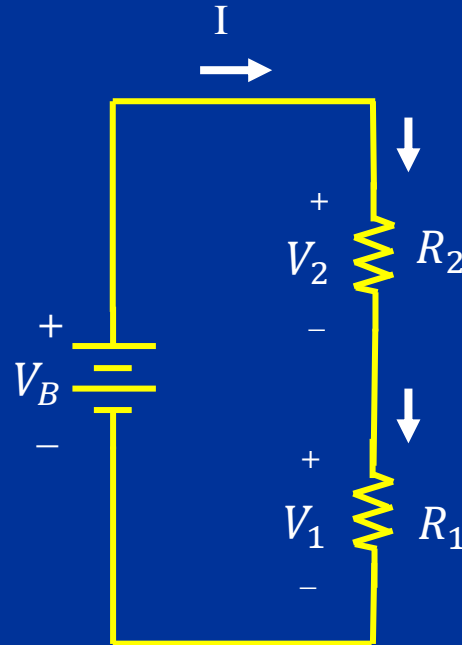
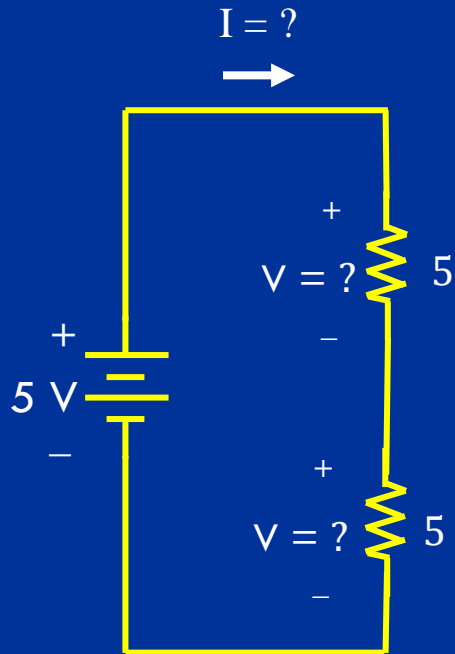
A Simple Example with 2 Resistors



Generalizing the Problem



Applying the Laws



KVL : $V_B = V_2 + V_1$

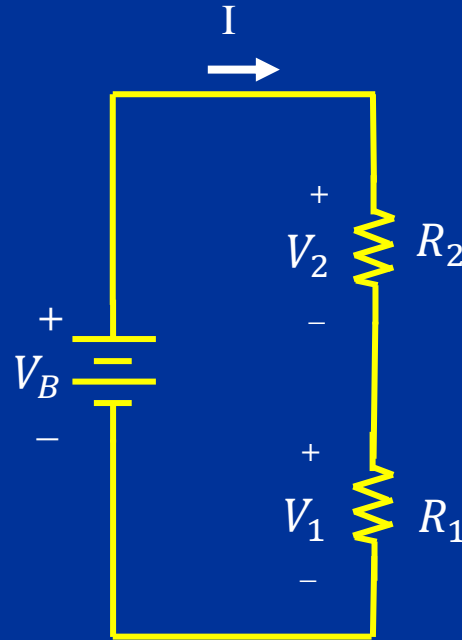
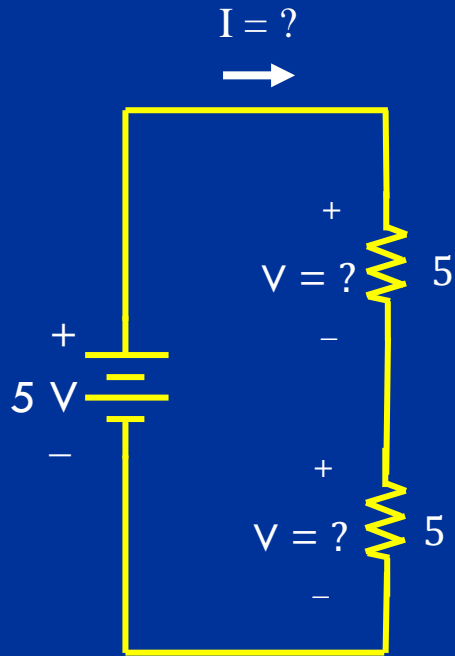
Ohm's Law : $V_2 = I_2 R_2$

Law : $V_1 = I_1 R_1$

KCL : $I = I_2 = I_1$

I_1

Solving the Equations



KVL : $V_B = V_2 + V_1$

Ohm's $V_2 = I_2 R_2$

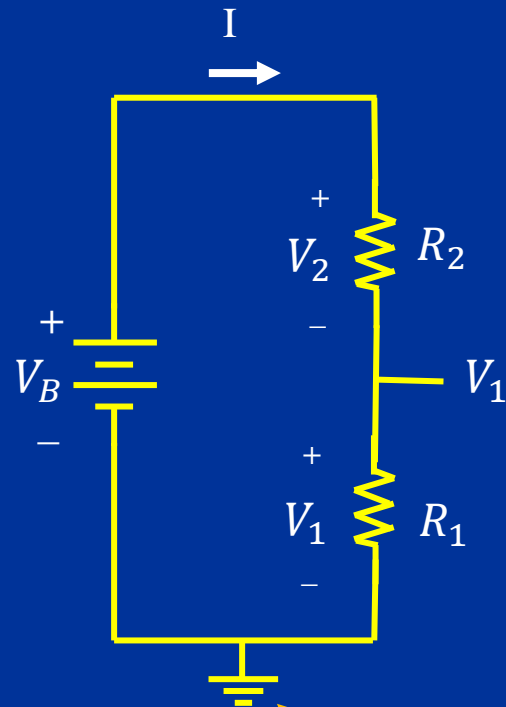
Law : $V_1 = I_1 R_1$

KCL : $I = I_2 = I_1$

Solve to get :

$$I = \frac{V_B}{R_1 + R_2} = 0.5 \text{ A}$$
$$V_1 = V_B \frac{R_1}{R_1 + R_2} = 2.5 \text{ V}$$
$$V_2 = V_B - V_1 = 2.5 \text{ V}$$

Some Useful Results



The Series Resistance formula

$$I = \frac{V_B}{R_1 + R_2}$$

“Voltage Divider” equation

$$V_1 = V_B \frac{R_1}{R_1 + R_2}$$

The “Voltage Drop” concept

$$V_1 = V_B - I R_2$$

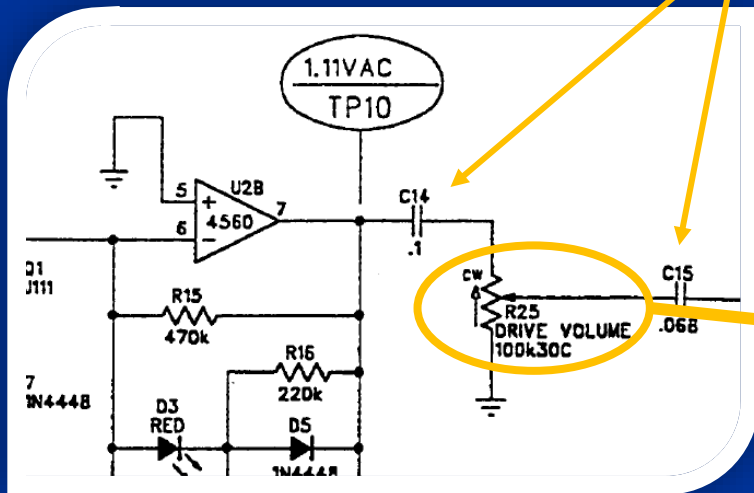
Ground (aka Reference-node)

Potentiometer (Voltage-Divider) Classic Volume Control



<https://reverb.com/p/fender-champion-30-2-channel-30-watt-1x10-guitar-practice-amp-1999-2002>

AC coupling capacitors (aka DC blocks)



<https://music-electronics-forum.com/filedata/fetch?id=832608>

Potentiometer

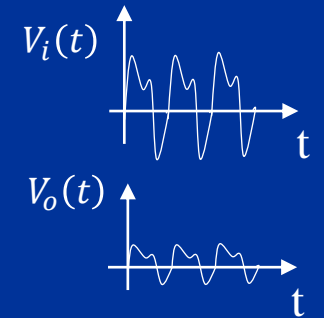
A typical single-turn potentiometer

Type: Passive

Electronic symbol (IEC Standard)

(ANSI Standard)

<https://en.wikipedia.org/wiki/Potentiometer>

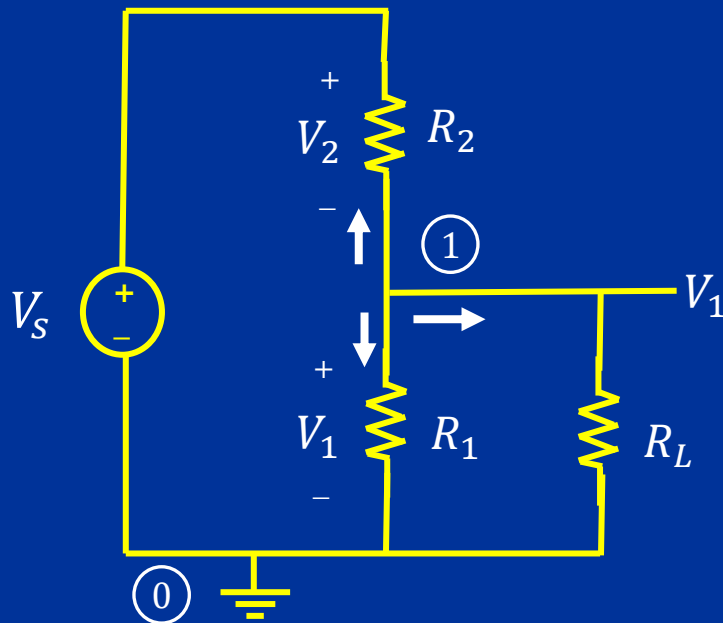


Pots Used for Reverb and Tone Adjust Too



A More Complicated Example (Loaded voltage-divider)

KCL-based “Nodal Analysis” at node 1 : $\sum I_{leaving-node-1} = 0$



$$(V_1 - V_S) \frac{1}{R_2} + V_1 \left(\frac{1}{R_1} + \frac{1}{R_L} \right) = 0$$

$$\Rightarrow V_1 = V_S \frac{1}{1 + \frac{R_2}{R_1} + \frac{R_2}{R_L}}$$

Checks:

$$R_2 \rightarrow 0 \Rightarrow V_1 = V_S \quad \checkmark$$

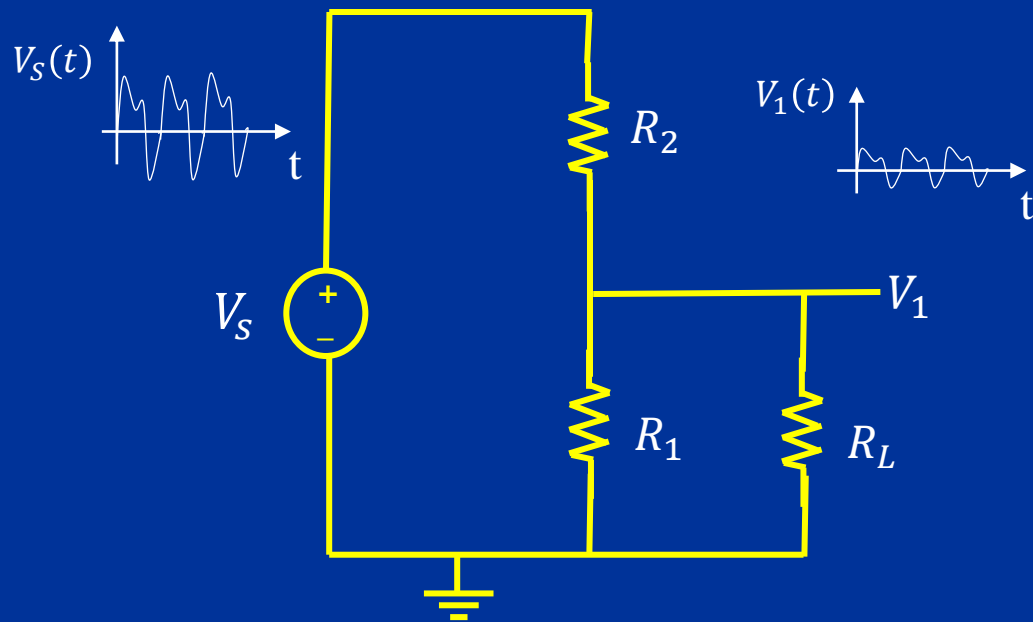
$$R_L \rightarrow \infty \Rightarrow V_1 = V_S \frac{1}{1 + \frac{R_2}{R_1}} = V_S \frac{R_1}{R_1 + R_2} \quad \checkmark$$

NOTE: Simulators such as SPICE handle large circuits using “Modified Nodal Analysis” and solve simultaneous equations using matrix math

But this isn’t the most human-friendly, or insightful approach ...

A “Better” Approach 😊

Leverage already known V-divider and Parallel-R results...



$$V_1 = V_S \frac{R_{eq}}{R_{eq} + R_2}$$

where $R_{eq} = R_1 \parallel R_L = \frac{1}{\left(\frac{1}{R_1} + \frac{1}{R_L}\right)}$

NOTE: if $R_L \gg R_1$ then $R_{eq} \approx R_1$

An important simplification !

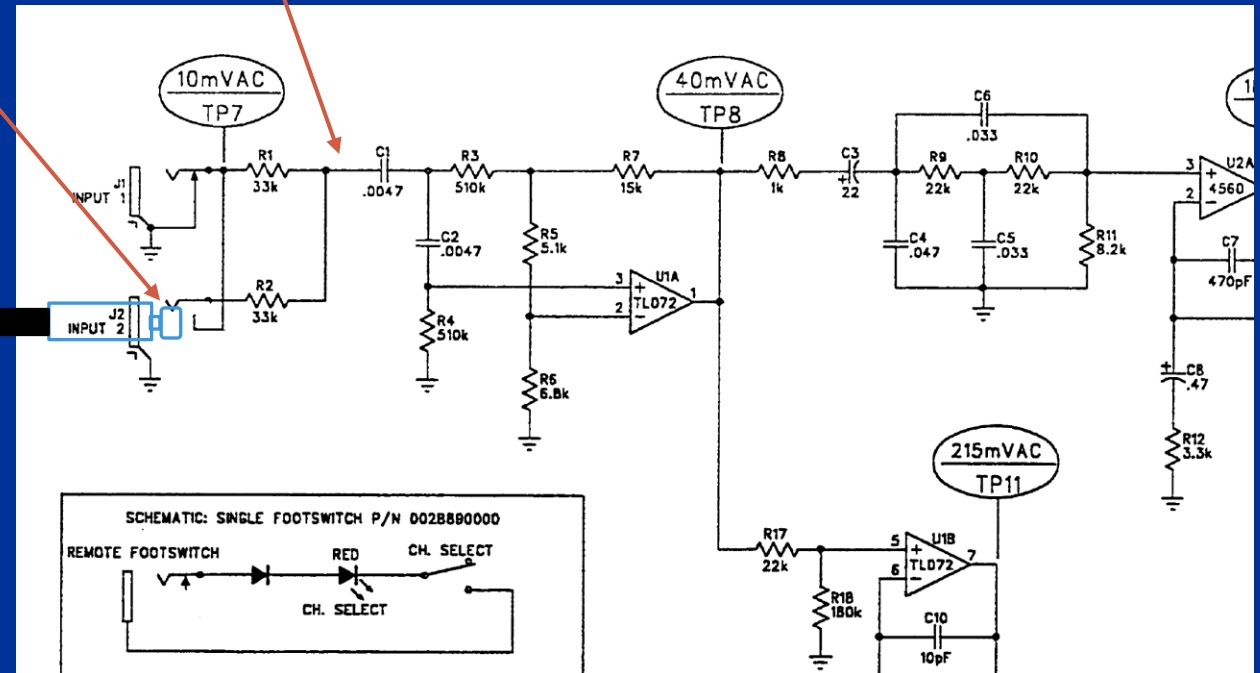
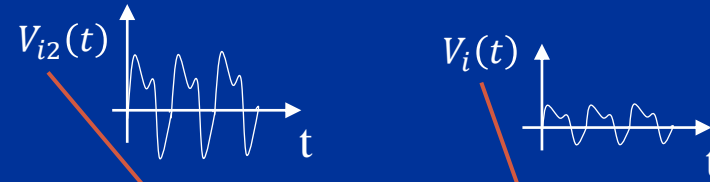
These are additional results we can now add to our mental circuits catalog !

Real-World Circuits

Example: Fender "Champion 30" Guitar Amp



<https://reverb.com/p/fender-champion-30-2-channel-30-watt-1x10-guitar-practice-amp-1999-2002>



<https://music-electronics-forum.com/filedata/fetch?id=832608>

Parsing and Understanding Circuits

Example: Fender “Champion 30” Guitar Amp

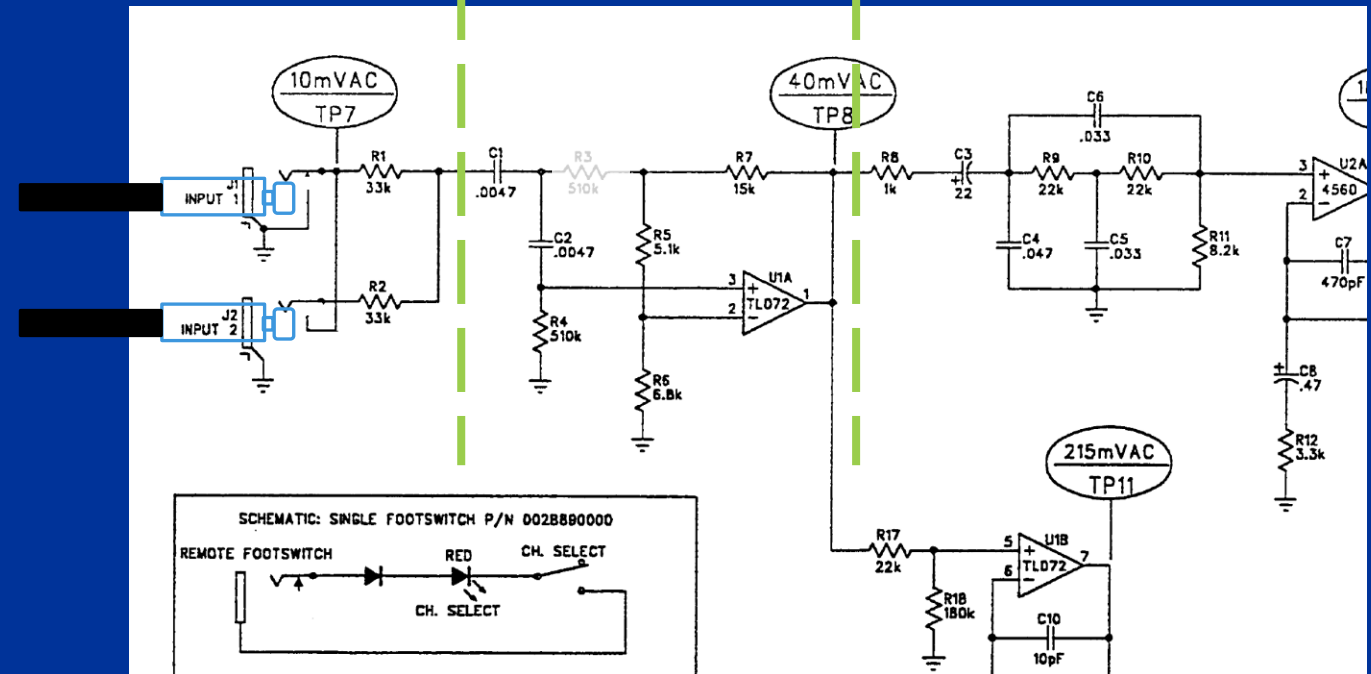


<https://reverb.com/p/fender-champion-30-2-channel-30-watt-1x10-guitar-practice-amp-1999-2002>

Signal-Summing
Circuit

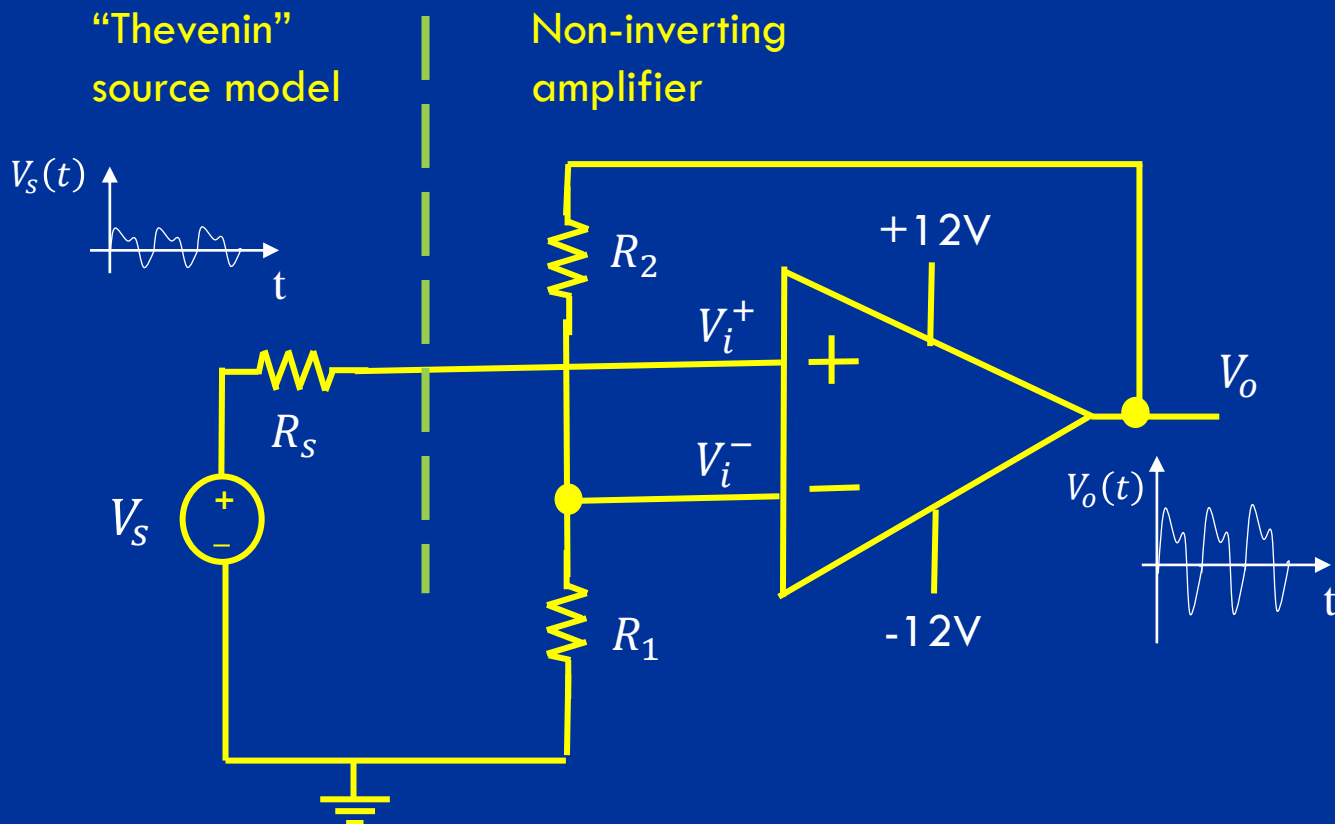
Opamp-based
Voltage amplifier

Frequency Response
Shaping



<https://music-electronics-forum.com/filedata/fetch?id=832608>

Non-inverting Opamp Voltage Gain Stage



Use known V-divider,

$$V_i^- = V_o \frac{R_1}{R_1 + R_2}$$

and near-infinite
"open-loop" gain
approximation...

$$V_i^- \approx V_i^+$$

To find output,

$$\Rightarrow V_o = V_i^+ \left(\frac{R_1 + R_2}{R_1} \right)$$

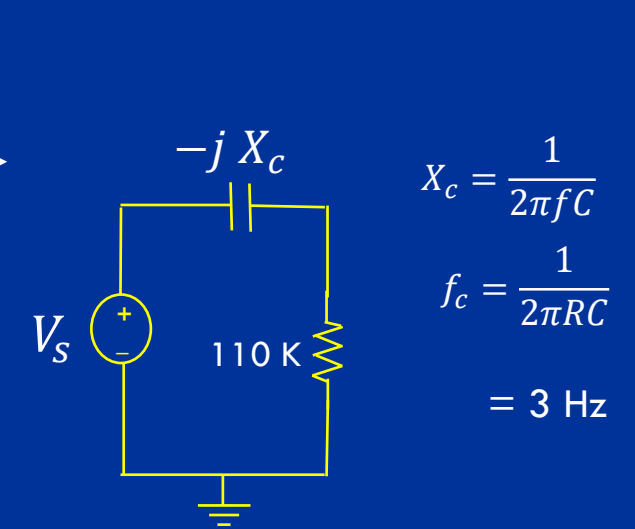
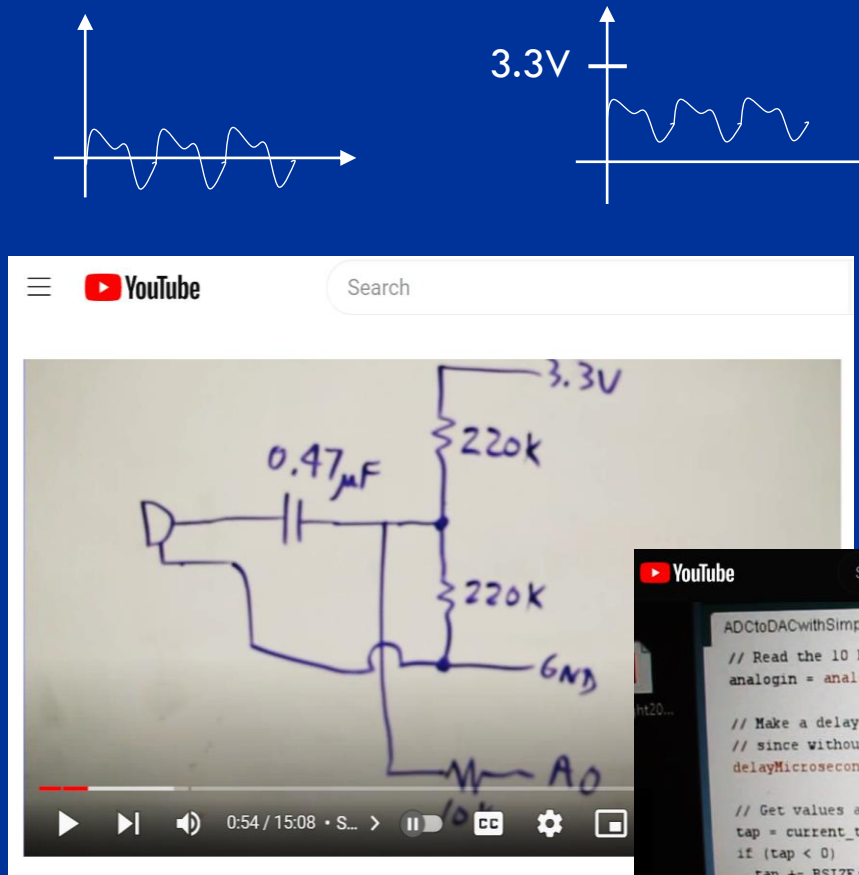
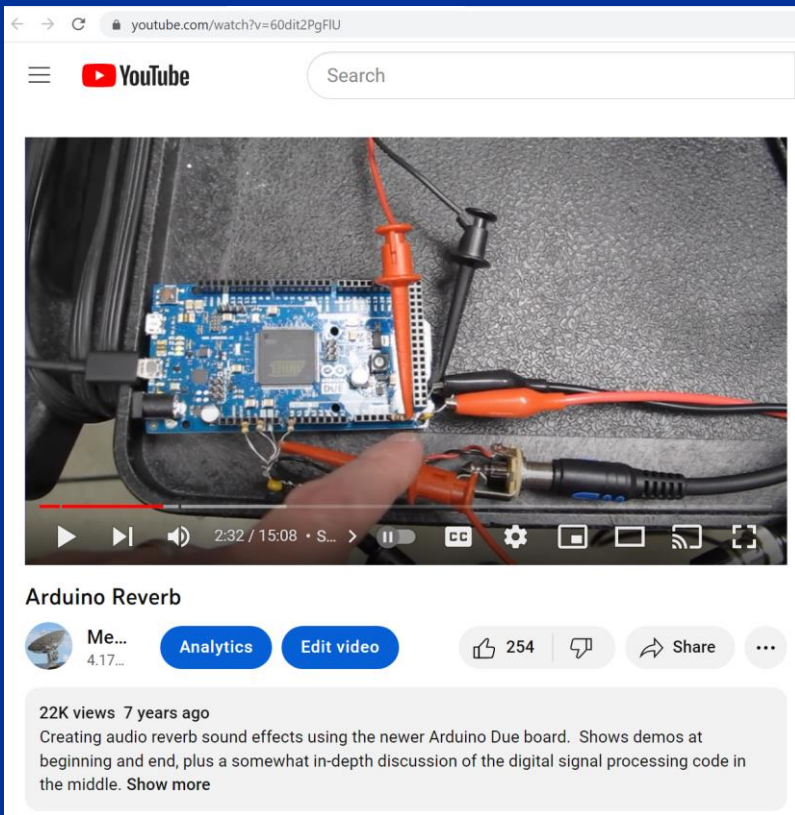
and "closed-loop"
voltage gain:

$$\Rightarrow A_v = \frac{V_o}{V_i} = \boxed{1 + \frac{R_2}{R_1}}$$

This is another common circuit, used in the amplifier example, with embellishment...

Designing New Circuits

Example: Audio Input Level-Shifter for Arduino



```
ADCToDACwithSimpleTwoTapReverb_Rev_Due1c$
// Read the 10 bit analog value on pin A0 and convert to bipolar values
analogIn = analogRead(A0) - 2048;

// Make a delay of about 20 us so sample rate is 40 Ksamp/sec
// since without delay it seems to sample >= 100K/sec
delayMicroseconds(20);




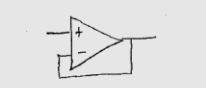
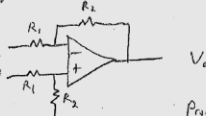
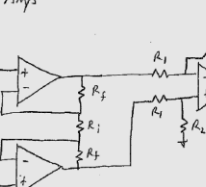
// Get values at delayed tap points in buffer
tap = current_tap - T1;
if (tap < 0)
    tap += BSIZE;
old_value = ring_buff[tap];

tap = current_tap - T2;
```

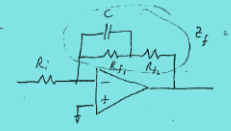
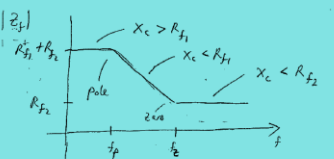

Possible Future Videos

- More circuit analysis techniques (e.g. Thevenin circuits and linearity)
- Opamp circuit catalog
- DC vs midband (AC) circuit analysis
- Complex impedances, frequency response, and Fourier analysis
- Power amps
- Power supplies, ...

Op Amps Circuit Catalog

- 1) Inverting Amp:  $V_o = -\frac{R_f}{R_1} V_i$ (if $R_i = R_1$, $R_o = 0$)
- 2) Inverting Summing Amp:  $V_o = -\left[\frac{R_f}{R_1} V_1 + \frac{R_f}{R_2} V_2 + \frac{R_f}{R_3} V_3\right]$
- 3) Non-inverting Amp:  $\frac{V_o}{V_i} = 1 + \frac{R_f}{R_1}$
 $R_i = \infty$, $R_o = 0$
- 4) Buffer Amp:  $\frac{V_o}{V_i} = 1$
 $R_i = \infty$, $R_o = 0$
- 5) Difference Amp:  $V_o = \frac{R_2}{R_1} (V_{i1} - V_{i2})$
Prod: Use superposition
- 6) Instrumentation Amp:  $V_o = \dots$

8) Bass Boost


 $Z_f = \frac{R_f}{1 + sR_1C} + R_1$
 $\frac{V_o}{V_i} = -\frac{Z_f}{R_1}$
 $X_C = \frac{1}{2\pi fC}$


$f_p = \frac{1}{2\pi R_1 C}$
 $f_z = \frac{1}{2\pi (R_1 + R_f) C}$

THANKS FOR WATCHING !